

Definitions: Function – A mathematical relation where each value of x only gives ONE (at most) values of y

Domain – All of the x values that CAN be put into a relation

Range – All of the y values that CAN be produced by a function

Vertical line test for a function:

Draw vertical lines through the graph. If any of the lines intersect the graph MORE THAN ONCE, it is NOT a function. Otherwise, it is.

Ex. Graph the relations shown in each of the following tables of values, then

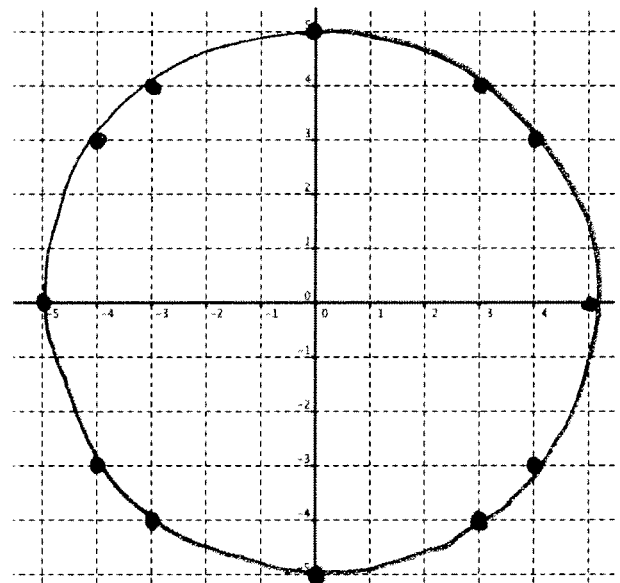
- write an equation for each relation
- label all x-intercepts and y-intercepts
- state the domain and range of each relation
- indicate which relation(s) are not functions based on their table(s) of values and graph(s)

a)

x	y
-5	0
-4	-3
-4	3
-3	-4
-3	4
0	-5
0	5
3	-4
3	4
4	-3
4	3
5	0

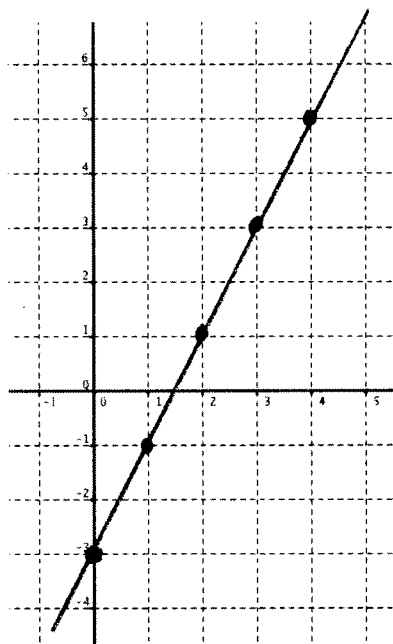
$$D: \{-5 \leq x \leq 5\}$$

$$R: \{-5 \leq y \leq 5\}$$



b)

x	y
-1	-5
0	-3
1	-1
2	1
3	3
4	5
5	7



$$D: \{x \in \mathbb{R}\}$$

$$R: \{y \in \mathbb{R}\}$$

c)

x	y
0	5
1	0
2	-3
3	-4
4	-3
5	0
6	5



$$D: \{x \in \mathbb{R}\}$$

$$R: \{y \geq -4\}$$

We use function notation to indicate which variable is the "input" or independent variable:

This allows us to show the "y" value of a function and the "x" value that it depends on.

If $f(x) = x^2 - 9$

"a function of x is equal to x squared minus nine"

Then $f(4) =$

"the value of the function when x (the input) is four"

or "f at 4 equals" or "f of 4 equals"

Ex. Use function notation to determine "the value of each function at each x-value."

a) For $f(x) = 3x - 5$:

$$\begin{aligned} f(-4) &= 3(-4) - 5 \\ &= -12 - 5 \\ &= -17 \end{aligned}$$

$$\begin{aligned} f(0) &= 3(0) - 5 \\ &= -5 \end{aligned}$$

b) For $g(x) = 2x^2 - x - 3$:

$$\begin{aligned} g(-1) &= 2(-1)^2 - (-1) - 3 \\ &= 2 + 1 - 3 \\ &= 0 \end{aligned}$$

$$\begin{aligned} g\left(\frac{3}{2}\right) &= 2\left(\frac{3}{2}\right)^2 - \left(\frac{3}{2}\right) - 3 \\ &= 2\left(\frac{9}{4}\right) - \frac{3}{2} - 3 \\ &= \frac{9}{2} - \frac{3}{2} - \frac{6}{2} \\ &= 0 \end{aligned}$$